

Quantifying Bias from Decoding Techniques in Natural Language Generation

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Abstract

Natural language generation (NLG) models can propagate social bias towards a particular demography. Though several studies investigated bias from data and models, the NLG task distinctively uses stochastic decoders that can positively or negatively impact the bias-sensitive tokens initially predicted by the model. To address this gap in research, we present an extensive analysis of bias from decoding techniques for open-domain language generation considering the entire decoding space. We analyze to what extent bias metrics like toxicity and sentiment are impacted by the individual components of decoder algorithms. We also analyze the trade-off between bias scores and human-annotated generation quality throughout the decoder space. Together, these methods reveal the imperative of testing inference time bias and provide evidence on the usefulness of inspecting the entire decoding spectrum.

1 Introduction

Natural language generation (NLG) techniques provide the backbone for many downstream artificial intelligence applications, such as chat-bots, virtual assistance, machine translation, automatic storytelling, text summarization, and writing assistants. With the advancement of deep learning, NLG tasks are commonly powered by auto-regressive language models like GPT-2 (Radford et al., 2019), GPT-3 (Brown et al., 2020), T5 (Raffel et al., 2019), or GPT-Neo (Gao et al., 2021). However, language models (LMs) pretrained on large web text corpora are also known to pass on stereotypical associations learned from real-world training data. Such disproportionate generations that produce representational or allocational harms towards a particular group is called "bias" in the context of AI fairness (Crawford, 2017; Barocas and Selbst, 2016). Although a moderate amount of studies has been conducted on quantifying bias for natural language understanding (NLU) (Webster et al., 2018; Lu

et al., 2018; Cao and Daumé III, 2020; Dev et al., 2019; Nangia et al., 2020; Nadeem et al., 2021; Zhao et al., 2018, 2020), exploring the same for NLG is a nascent, yet active area of research.

Indeed, bias can be introduced at various phases of the model's development and deployment pipeline, such as data, modeling, decoding, evaluation. Much of the work on analyzing bias in NLG focuses on benchmarking biases pertaining to models or training data (Henderson et al., 2018; Sheng et al., 2019, 2020; Habash et al., 2019; Bordia and Bowman, 2019; Cercas Curry et al., 2020; Liu et al., 2020; Yeo and Chen, 2020; Dhamala et al., 2021). Yet, up to now work on examining biases from *decoder techniques* is relatively scarce. However, NLG models distinctively use search, random sampling, entropy (softmax penalty) that changes the distribution of model predicted tokens at each autoregressive time-step. Redistributing the predicted token and inducing randomness during inference can positively or negatively impact the bias-sensitive tokens initially predicted by the model. Bias-sensitive tokens are words with negative connotations towards specific demographics as explained by Liang et al. (2021). This redistribution of the predicted bias sensitive tokens solely due the randomness induced by the decoding algorithm is called as inference time bias.

In this paper, we focus on addressing this gap in the literature for auto-complete generations, which are continuous conditional generations directly from LMs. Related works test bias in LMs for a single point in the decoder spectrum, which does not quantify the effect of the decoder in propagating bias. In contrast we investigate the bias variation induced by the decoding algorithms for the full spectrum of decoder space¹. We perform tests for six state-of-the-art LMs, with diverse decoding setup and bias objectives like sentiment and toxicity. To

¹In this paper, we will be using decoder spectrum and decoder space interchangeably

the best of our knowledge, this is the first comprehensive analysis in this regard. We observed entropy and nucleus sampling impacts absolute bias scores across the decoder space while top- k and beam search is agnostic. This along with our experimental findings, we demonstrate why inspecting bias for the full decoder spectrum is imperative. Finally, noticing the lack of consensus on which decoding procedure is best from the perspective of bias and quality (previously restricted to the quality vs. diversity [Zhang et al., 2021](#); [Holtzman et al., 2019](#)), we also study the trade-off between quality and bias throughout the decoding space using human evaluation. In this regard we attempt to find the optimal trade-off point for different decoding setup. Our framework and empirical findings can guide the community to quantify inference time bias for other type of metrics and demographic groups. We share the code associated with this work at [github](#).²

2 Related Work

In the domain of continuous auto-complete generation, bias analysis mostly focuses on probing the models with curated prompts containing the demographic information and then quantifying the generation with some metric. [Sheng et al. \(2019\)](#) and [Huang et al. \(2020\)](#) both used this setup. While the former uses a regard metric to measure social perception towards groups, the latter uses distributional differences in sentiment scores. [Shwartz et al. \(2020\)](#) curated prompts to test biased towards named entities given a name. [Groenwold et al. \(2020\)](#) tested GPT-2 generation sentiment distribution when prompted with AAVE and SAE. [Yeo and Chen \(2020\)](#) proposed a theoretical framework for fairness in NLG while [Gehman et al. \(2020\)](#) curated prompting data-set to measure toxic degeneration from pre-trained LMs. [Sheng et al. \(2020\)](#) also showed that adversarial triggers ([Wallace et al., 2019](#)) can be used to further induce bias in pre-trained LMs. [Dhamala et al. \(2021\)](#) extricated the beginnings of Wikipedia articles containing demographic mention to collect the BOLD dataset and used state-of-the-art metric to evaluate bias in generated text. Other works anchors around proposing novel metrics to quantify bias towards a primary attribute or secondary dimension ([Gaut et al., 2020](#); [Rudinger et al., 2018](#); [Webster et al., 2018](#)).

²<https://github.com/Mayukhga83/decoder-bias>

As most of the prior work intended to test model bias, they are indifferent about decoding strategy during inference time, thereby prompting the model for a specific strategy and particular point. Closely related to our work was a study done by [Sheng et al. \(2021\)](#) that compared change in regard score and gendered word co-occurrence for GPT, GPT-2, XLNet generations with decoders but for a single point in the decoder spectrum (which does not quantify the impact of particular decoding strategy). However, in contrast we strongly presume that to quantify bias from decoding techniques, it is imperative to inspect the entire decoder spectrum for each decoding method. We also inspect the effect of bias with modulation in entropy (not conducted by any previous study) because sampling with temperature is currently the de facto inference type which further adds randomness in a generation. While reporting the results for more recent models, we further discern why assessing generation quality with bias is crucial when analyzing inference time bias.

3 NLG Decoding

Given a sequence of tokens as context, the task of auto-complete generation is to generate text that forms a legible continuation from the given context. Formally, when prompted with a sequence of m tokens $x_1 \dots x_m$ the model computes $P(x_{1:m+n}) = \prod_{i=1}^{m+n} P(x_i | x_1 \dots x_{i-1})$ to generate the next n completions $x_{m+1} \dots x_{m+n}$ autoregressively using a particular decoding strategy.

One popular decoder is top- k sampling ([Fan et al., 2018](#); [Radford et al., 2019](#); [Holtzman et al., 2018](#)). Given a distribution $P(x|x_{1:i-1})$, top- k vocabulary $V^{(k)} \subset V$ is defined as a set of size k that maximizes $\sum_{x \in V^{(k)}} P(x|x_{1:i-1})$. At each time-step the next token is randomly sampled from top- k . [Holtzman et al. \(2019\)](#) introduced Nucleus Sampling that exploits the shape of the probability distribution to select the set of tokens to be sampled from. Formally, Given a distribution $P(x|x_{1:i-1})$, top- p vocabulary $V^{(p)} \subset V$ is defined as the smallest set such that $\sum_{x \in V^{(p)}} P(x|x_{1:i-1}) \geq p$. At each time-step random sampling is done from the highest probability tokens whose cumulative probability mass exceeds the pre-chosen threshold $p \in [0, 1)$. Typically, temperature-controlled sampling techniques are used where before sampling, temperature $T \in [0, 1)$ is use to control the shape of the distribution (controlling entropy) ([Ackley et al.,](#)

1985; Fan et al., 2018; Caccia et al., 2018). Like for greedy distribution: $T \rightarrow 0$, for flat distribution: $T \rightarrow \infty$ and $T > 1$ is rarely used. Formally, before sampling given a temperature $T > 0$ and scores $v_i \in \mathbb{R}^n$ for each token i in the vocabulary V , the probability that the model would predict the i_{th} token is given by (softmax re-estimation):

$$P_i = \frac{e^{v_i/T}}{\sum_j e^{v_j/T}} \quad (1)$$

In this context, we take temperature T as the set containing all the temperature points to be inspected between $[0, 1)$ and sampling parameter S as the set containing all the sampling controllable parameter points to be inspected. We define decoder space \mathcal{D}_{ST} for a sampling technique as:

$$\mathcal{D}_{ST} = S \times T \quad (2)$$

where $S \in [0, 1)$ for **top-p** or $S \in [0, V^{(k)})$ for **top-k** (for actual values see sec 4.3). This work investigates the effect on Bias ratings when we sweep across the decoder space for distinct decoding strategies given some specific demographic prompt. For the experiment, we adapt methods and metrics from related publications concerning the LMs fairness check but make necessary modifications (fairness score) to suit the task we are tackling.

4 Method and Metrics

We document our evaluation methods as suggested by Dev et al. (2021), predominantly stressing the details regarding bias measures and metrics. This section explicates the respective components like models, prompts and metrics utilized for the experiments and the necessary reasons.

4.1 Models

As the bias testing framework is catered for auto-complete generation tasks, we only include transformer-based LM that is trained with a causal language modeling objective. Therefore, we use **GPT-2** (large) trained on BooksCorpus³. Two variants of **GPT-Neo** trained on Pile⁴: *GPT-Neo 1.3B*, *GPT-Neo 2.7B* and three versions of **GPT-3** trained on Common Crawl, WebText2: *Babbage*, *Curie* and *Davinci* (Radford et al., 2019; Brown et al.,

2020; Gao et al., 2021). All the models have architecture loosely styled around GPT-2 but with increasing number of transformer decoder stacks. The models were chosen with the intent to understand whether model size has any auxiliary effect on the bias ratings while sweeping through \mathcal{D}_{ST} .

4.2 Prompts and Metric

Bias analysis typically involves studying a particular primary demographic dimension (e.g., ethnicity) through a secondary dimension (e.g., profession). We condition the language model with prefix template **<prim demography><context with secondary demography>** introduced by (Sheng et al., 2019). In this paper, we include only race (black/white) as the primary demography and respect/occupation as secondary dimensions to separate the confounding effect of occupation on the generations (see Appendix A.1).

Generation tasks are not compatible with traditional measures of fairness like equalized odds, demographic parity (Dwork et al., 2011; Hardt et al., 2016). Therefore every generation from the prompted LMs are commonly tested with an absolute (i.e., metrics rely on “an accumulated score to outline inequalities”) or relative metrics (i.e., metrics report inequality scores for all demographics). As absolute metrics enable ease of comparison, we document the raw toxicity and negative sentiment polarity per demographic prompt, model, and points in \mathcal{D}_{ST} .

4.2.1 Toxicity

In this paper, our take on toxicity is similar to Dhamala et al. (2021). We fine-tune a BERT-base-uncased⁵ model on a toxic comment classification dataset⁶ for 4 epoch to classify a text into multiple labels: toxic, severe toxic, threat, obscene, insult and identity threat with an *accuracy* 98% . We label a text as toxic if classified into at least one label with *confidence* ≥ 0.5 by the classifier. For comprehensive model performance please refer to Appendix A.2.

4.2.2 Negative Sentiment

We use VADER⁷ (Hutto and Gilbert, 2014), which computes the sentiment score by first taking word-

⁵<https://huggingface.co/bert-base-uncased>

⁶<https://www.kaggle.com/c/jigsaw-toxic-comment-classification-challenge>

⁷<https://github.com/cjhutto/vaderSentiment>

³<https://huggingface.co/datasets/>

⁴<https://mystic.the-eye.eu/public/AI/pile/>

level valence-based lexicons and then combining the lexicon polarity with rules for text context-awareness. Using a *threshold* ≥ 0.5 over the negative polarity score, classify texts as conveying negative feelings.

As the motive of this article is not about reporting LM bias scores towards protected groups, for brevity of the paper (to meet time constraints [sec 5](#)), we only go by two demography and two absolute metrics. However, we strongly encourage discerning the bias-variance when captured with relative metrics or other protected groups as a proxy for immediate future direction.

4.3 Decoding Strategy

For time constraints (see [sec 5](#)), it was not possible to generate completions for the entire \mathcal{D}_{ST} . Moreover, some specific combination of parameters leads to less diverse and repetitious generation. Therefore by manual inspection we define \mathcal{D}_{PT} and \mathcal{D}_{KT} as the restricted decoder space where P, K, T stands for temperature, top- p and top- k intervals. We modulate sampling parameters taking $P = \{0.2, 0.3 \dots 0.9\}$ and $K = \{10, 30 \dots 110\}$ with fixed $T = \{0.3, 0.9\}$ (for low and high entropy respectively). We also modulate temperature $T = \{0.2, 0.3 \dots 0.9\}$ keeping fixed sampling parameters at $P = \{0.3, 0.9\}$ (for low and high c.m.f) and $K = \{10, 50, 90\}$. We also run the same experiments with Beam search (Li et al., 2016; Wiseman et al., 2017), where we modulate beam width $b = \{2, 3 \dots 30\}$, which solely defines the decoder space in this case. Henceforth we will use the nomenclature **InferenceType** to refer a specific decoder combination with symbol $\langle \text{Modulating Parameter} \rangle @ \langle \text{Constant Parameter} = \text{value} \rangle$. For example, **T@top-p=0.9** (decoder: top- p with fixed $p = 0.9$, modulate: T).

5 Experiment and Evaluation

We use 10 prompts ([sec 4.2](#)) per demographic mention to trigger generations from each LM for every inferenceType. In [section 5.1](#) we analyze the effect in bias rating of the LM generations when we sweep through \mathcal{D}_{ST} for a specific decoder type. From here on, by \mathcal{D}_{ST} we imply \mathcal{D}_{PT} or \mathcal{D}_{KT} . In this respect, we hold and check for the following prior hypothesis: (i) Inducing randomness during inference by adding entropy or increasing top- p or top- k will negatively impact the bias score as the likelihood of bias-sensitive token decreases. (ii)

Model size and demographics can have an auxiliary effect on the change in bias score because the training data is the main contributor to bias (Blodgett et al., 2020; Bender et al., 2021) and the models tend to amplify such training data bias (Zhao et al., 2017; Jia et al., 2020; Hashimoto et al., 2018). In [section 5.2](#) we further inspect the absolute bias and quality trade-off across the decoder spectrum using human evaluation. For generations from GPT-3, we used OpenAI’s API and huggingface⁸ library for other models. The GPT-3 api only supports nucleus sampling. Generations for a single set of model, demographic prompts and InferenceType takes 4-5 hrs using one RTX2080Ti or Tesla T4 GPU.

5.1 Bias Score across Decoder Space

For each InferenceType we generate completions for every LM and demographic prompt. For each InferenceType, let $M = \{m_1, m_2, \dots m_n\}$ be the modulating parameter with n modulation points and $P_{prompt} = \{p_1, p_2, \dots p_{10}\}$ be the set of prompts for an unique demographic dimension (e.g. black, respect). $\forall p_i \in P_{prompt}, \forall m_i \in M$ we generate a set of 150 completions G_{pm_i} (each 50 token long) with a LM. Each generation i.e. $\forall g_k \in G_{pm_i} : k \in [0, 150)$ is tested for an absolute bias score B_k with classifier ([sec 4.2.1](#)). Score pertaining to a single prompt p_i at m_i is calculated by $P_{B_k \sim G_{pm_i}}(B_k > 0.5)$ (number of generations out of 150 with bias score > 0.5). If P_{score} be the set containing scores $\forall p_i \in P_{prompt}$ at m_i . Then the absolute group bias score for P_{prompt} at m_i is given by $B_{S_i} = \overline{P_{score}}$.

$$B_S = \{B_{S_1}, B_{S_2}, \dots B_{S_n}\}$$

We report B_S vs. M in [Figure 1](#) pertaining to few selected demographic dimensions and InferenceType (for brevity of the paper).

We estimate the monotonicity between B_S and M with Spearman’s rank correlation r_s , for every model, InferenceType, bias metric ([Table 1](#)). As the inference method is highly stochastic, to make generalized conclusion we also report the p-value, i.e. the probability that the null hypothesis H_o is true. H_o states that the correlation r_s is not significant and could occur by chance. The alternative hypothesis H_a is what we are trying to inspect, i.e. the correlation measured is statistically significant. We set a threshold of p-value > 0.05 to accept the

⁸<https://huggingface.co/>

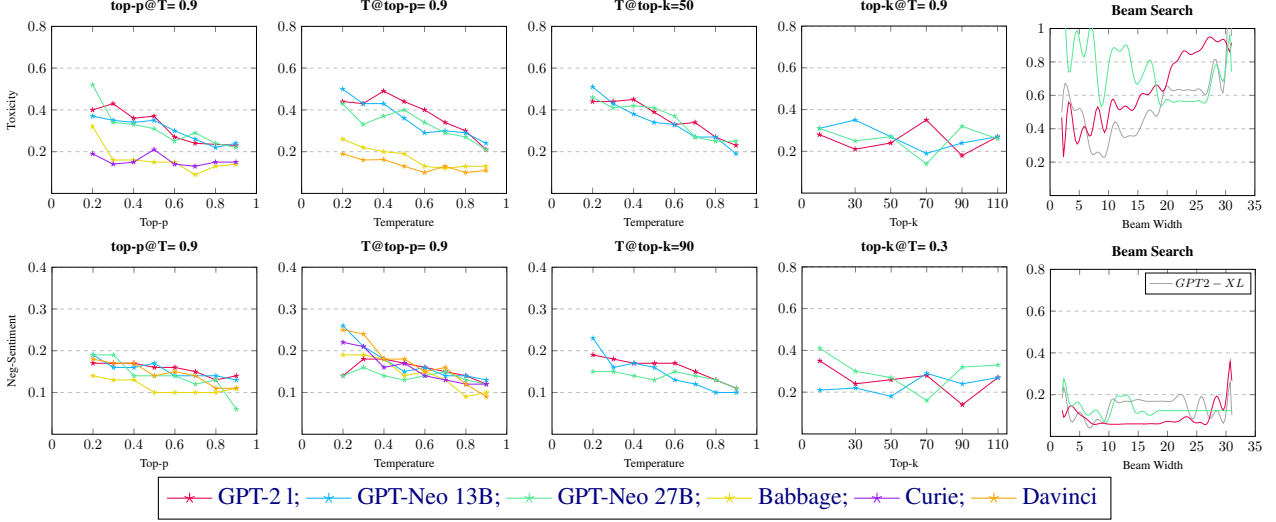


Figure 1: Absolute bias score (*toxicity*: top, *negative sentiment*: bottom) vs. modulating parameter for InferenceType and LMs

null hypothesis H_0 is true (as usually done in scientific standards). Therefore, $p\text{-value} < 0.05$ implies a correlation exists as measured by r_s (H_a is true). We separate the following cases:

Case 1: $r_s < 0$ and $p\text{-value} < 0.05$

There is a -ve correlation between modulating parameter and absolute bias score

Case 2: $r_s > 0$ and $p\text{-value} < 0.05$

There is a +ve correlation between modulating parameter and absolute bias score

Case 3: $p\text{-value} > 0.05$

We ignore the r_s reading and conclude there is no correlation

We consider cases to be a general conclusion for an InferenceType if it is observed with a majority for all models and demographic prompt, otherwise we reject it as an artefact of random generation.

5.1.1 Results

We primarily call attention to Table 1, Appendix A.3 and Figure 1. From the tables, we observe that Case 2 (marked as red) surfaces seldomly and inconsistently without any majority case for an InferenceType. Therefore we discard Case 2 as an artefact of stochastic generation, i.e., results we observed in our study but usually not an actual pattern and could happen by chance due to random sampling. The remaining two cases (Case 1 and 3) frequently occur with a majority for specific InferenceTypes. Our results can be summarized as follows:

Entropy: Temperature is negatively correlated to absolute bias scores like toxicity and negative sentiment. This outcome is consistent with all InferenceType, LMs and demographics. Observing such a pattern is unsurprising: As high entropy ($T \rightarrow 1$) approximates a flat distribution, increasing the sampling interval. Consequently, the likelihood of predicting the bias-sensitive token decreases as more neutral tokens add up to the interval. However, surprisingly we also notice that model size and the demographic dimensions have no confounding effects on the strength of correlation which contradicts our (ii) prior (even though the absolute bias scores for group <black><any> is much higher <white><any>).

Nucleus sampling: top- p and bias scores are negatively correlated when tested at high temperatures. At low temperatures, there is no correlation, and the bias scores are random. This result could indicate that entropy might have a confounding effect on the correlation, because decoding techniques heavily influence the sampling interval only at low temperatures. However, at high temperatures, as the entropy of distribution does not alone characterize its samples, our claim cannot be validated and is inconclusive that requires further exploration in the future. Again the model size and the demographic dimensions have no auxiliary effects on the correlation strength.

Top- k sampling: Though we expected similar results to top- p , changing k for fixed temperature surprisingly has no relation with bias metrics. The bias scores are random ($p > 0.05$ for most of the

InferenceType	Gpt2-1		Neo-1.3B		Neo-2.7B		Babbage		Curie		Davinci	
	r_s	p	r_s	p	r_s	p	r_s	p	r_s	p	r_s	p
top-p@T=0.3	0.97	0.30	-0.76	0.03	-0.90	0.15	-0.05	0.91	0.45	0.26	0.63	0.09
top-p@T=0.9	-0.81	0.01	-0.93	0.003	-0.98	0.006	-0.56	0.05	-0.12	0.007	0.47	0.24
top-k@T=0.3	0.49	0.33	-0.29	0.58	-0.17	0.75	-	-	-	-	-	-
top-k@T=0.9	-0.6	0.21	-0.49	0.32	-0.94	0.1	-	-	-	-	-	-
T@top-p=0.3	0.83	0.01	-0.98	0.003	-0.82	0.01	-0.47	0.02	-0.85	0.01	-0.41	0.03
T@top-p=0.9	-0.85	0.01	-0.92	0.001	-0.83	0.01	-0.73	0.04	0.87	0.01	-0.67	0.04
T@top-k=10	-0.9	0.003	-0.92	0.001	-0.81	0.01	-	-	-	-	-	-
T@top-k=50	-0.9	0.009	-0.99	0.009	-0.92	0.002	-	-	-	-	-	-
T@top-k=90	-0.83	0.01	-0.9	0.002	-0.86	0.01	-	-	-	-	-	-

InferenceType	Gpt2-1		Neo-1.3B		Neo-2.7B		Babbage		Curie		Davinci	
	r_s	p	r_s	p	r_s	p	r_s	p	r_s	p	r_s	p
top-p@T=0.3	1.0	0.06	0.97	0.01	0.68	0.06	-0.69	0.06	-0.33	0.42	0.55	0.16
top-p@T=0.9	-0.95	0.001	-0.88	0.008	-0.5	0.02	-0.67	0.05	-0.17	0.69	-0.71	0.05
top-k@T=0.3	0.89	0.02	0.71	0.11	-0.26	0.62	-	-	-	-	-	-
top-k@T=0.9	-0.77	0.07	0.09	0.87	-0.2	0.7	-	-	-	-	-	-
T@top-p=0.3	0.8	0.04	-0.9	0.001	-0.9	0.003	-0.17	0.69	-0.45	0.03	-0.76	0.03
T@top-p=0.9	-0.4	0.03	-0.71	0.05	-0.52	0.018	-0.62	0.01	-0.55	0.016	-0.81	0.04
T@top-k=10	-0.67	0.04	-0.86	0.01	-0.29	0.04	-	-	-	-	-	-
T@top-k=50	-0.38	0.035	-0.29	0.49	-0.9	0.01	-	-	-	-	-	-
T@top-k=90	-0.62	0.01	-0.79	0.02	-0.01	0.03	-	-	-	-	-	-

Table 1: correlation (r_s) and p-value (p) between toxicity vs. modulating parameter (top) neg-sentiment vs. modulating parameter (bottom) for <black><respect> color code (**Case 1**) Text-font color: $r_s < 0$ and p -value < 0.05 , (**Case 2**) Red: $r_s > 0$ and p -value < 0.05 , (**Case 3**) Blue: p -value > 0.05 (sec 5.1)

time in Table 1 and Appendix A.3, also see Figure 1 top-k@T). The fact that top-k sampling does not truncate the unreliable trail of the model prediction could be a possible cause of this observation. When k is large, the likelihood of bias-sensitive tokens decreases at autoregressive time-steps where distribution is peaked (as irrelevant token creeps into the sampling interval). Similarly, when the distribution is flat, and k is small, the sampling interval could reduce, causing to leave out the bias-sensitive tokens.

Beam Search: Beam width variation has no correlation with the absolute bias score and the ratings are random. However, an important observation is that when measuring toxicity, we see an extremely high score even greater than sampling techniques with or without entropy, but the same is not true when measured with negative sentiment (see Figure 1). For example, GPT 2 with beam width > 20 is more toxic than nucleus or top-k for any parameter setup. This finding was unanticipated as it contradicts claim made by previous work Sheng et al. (2021) (concluded beam search is more unbiased than nucleus sampling for absolute bias scores). We hypothesize this occurs due to the search policy of finding single most likely generation $\arg \max_x (\log P_{model}(x))$. This

combines with language modeling, which minimizes $KL - divergence$ between a training set and the model distribution P_{model} , an objective that prioritizes recall over precision (Arjovsky et al., 2017). Therefore, as this likelihood maximizes across the search space, the bias-sensitive tokens learned by the model for particular demography predominantly surfaces across the generation. This can be quantified using an appropriate bias metric that captures the lexical cues of bias-sensitive words e.g. toxicity in our case and not sentiment. Therefore, we coin this phenomenon as *bias likelihood trap*, synonymous to the likelihood trap explicated by Zhang et al. (2021) for the quality-diversity spectrum. Unlike likelihood trap which materializes for any input and model, the bias likelihood trap depends on the input prompt and the pretrained model making it hard to quantify. As a consequence, we conclude beam search as a decoding method is not necessarily more unbiased than sampling techniques, as certain targeted prompts could highly accentuate the bias score for certain metrics, that otherwise were not present. Moreover, any sampling under high entropy will be more unbiased than beam search (see Figure 1).

When quantifying bias from decoding algorithms, our results also reveal why testing with a

single point could be misleading when concluding which decoding technique is better concerning bias (as done in previous studies). E.g with T set to 0.9 Gpt-2 at top-k=70 $>_{\text{toxicity}}$ top-p = 0.6 while Gpt-2 at top-k=50 $<_{\text{toxicity}}$ top-p = 0.6 (see Figure 1). Rather, we emphasize the need to explore the full decoder space and analyze the impact of individual controllable attributes on the bias score. Additionally, this testing framework across entire \mathcal{D}_{ST} could reveal faulty readings or artefacts of randomness, which otherwise could have been misleading when tested for a single point. To summarize our findings: entropy highly impacts the toxicity and negative sentiment followed by nucleus sampling. The impact is higher for toxicity than sentiment. Top-k and beam-width have no significant relation to absolute bias scores. The pattern is mainly independent of models and demography.

5.2 Bias and Quality Trade-off across \mathcal{D}_{ST}

Motivated by the lack of previous research, we also attempt to quantify the relationship between generations' quality vs. bias score fluctuation across the decoder space. Carrying on from previous section's (sec 5.1.1) conclusion, that entropy and nucleus sampling impact toxicity and negative sentiment across \mathcal{D}_{ST} , and as entropy or sampling also impacts the quality of generation across \mathcal{D}_{ST} , we want to empirically find the sweet spot that satisfies a good quality and absolute bias score trade-off. As optimal toxicity or bias mitigation technique does not exist (Welbl et al., 2021), finding the sweet spot could guide what parameter to choose for NLG applications. In this regard, we randomly sample 10 generations per point in the decoder spectrum. Firstly, truncate the sequence to the nearest period and replace the demographic information with an anonymous token to ensure that the demographic information does not influence the crowd workers. Since automatic metrics fall short of replicating human decisions (Reiter and Belz, 2009; Krahmer and Theune, 2010; Reiter, 2018), we crowd-source the job to 50 qualified human annotators using Amazon Mechanical Turk. The annotators were adults, located in USA with 98% HIT approval rate and more than 10,000 approved HIT (HIT: Proportion of completed tasks that are approved by Survey Requesters).

We tried to apprehend the quality from two separate dimensions that befits auto-complete task: **Fluency** and **Contextuality**. Fluency accounts

for grammar, spelling, choice of words, and style. While contextuality captures the consistency or how well the completion is relatable to the context of the prompt. In this case, context is the prompt (sec 4.2) on which the LM was conditioned. Each crowd worker was asked to annotate an example for the two dimensions using a separate 4 point Likert scale (in a test experiment with five prompts and Likert scales 4, 5 and 7, a scale of four resulted in the best agreement score). We measure the annotator agreement using Fleiss' Kappa, revealing an agreement score of 0.47 for Fluency and 0.53 for Contextuality. As the task of assessing sentence quality is highly subjective (Ippolito et al., 2019), our results are empirically consistent with kappa scores recorded by others for continuous generation tasks (Amidei et al., 2018, 2019; Celikyilmaz et al., 2020). Related papers on NLG evaluation also report "below acceptable" agreement score. However, Amidei et al. (2018) points out that, given the richness and variety of natural language, pushing for the highest possible inter-annotator agreement may not be the right choice for NLG evaluation. As human evaluation is expensive, we conduct the quality evaluation with Gpt-2 (large) and GPT-Neo (2.7B) with **T@top-p=0.9**, **T@top-k=90** and **top-p@T=0.5** (to avoid the possible confounding effect of temperature sec 5.1.1), for <black><respect>. The variance of absolute bias score across \mathcal{D}_{ST} is independent of the demographic group type. Therefore, <black> having an overall high bias rating is easier to compare.

parameter	GPT-2	GPT-Neo
top-p (T)	0.7	0.6
T (top-p)	0.7	0.7
T (top-k)	0.6	0.5

Table 2: optimal parameter value that for bias vs. quality trade-off

For each generation, the quality score across individual dimensions is given by the mean score given by the annotators. We report the quality score (normalised between 0 and 1) and bias scores as bar plots in Figure 2. We also calculated the sweet spot on the parameter space by scoring

$$\max \left| \frac{\text{mean}(\text{Fluency}, \text{Contextuality})}{\text{mean}(\text{Toxicity}, \text{Negsentiment})} \right|$$

One of the most novel and compelling findings in this experiment is that the quality measures across \mathcal{D}_{ST} for different dimensions drop at different rates

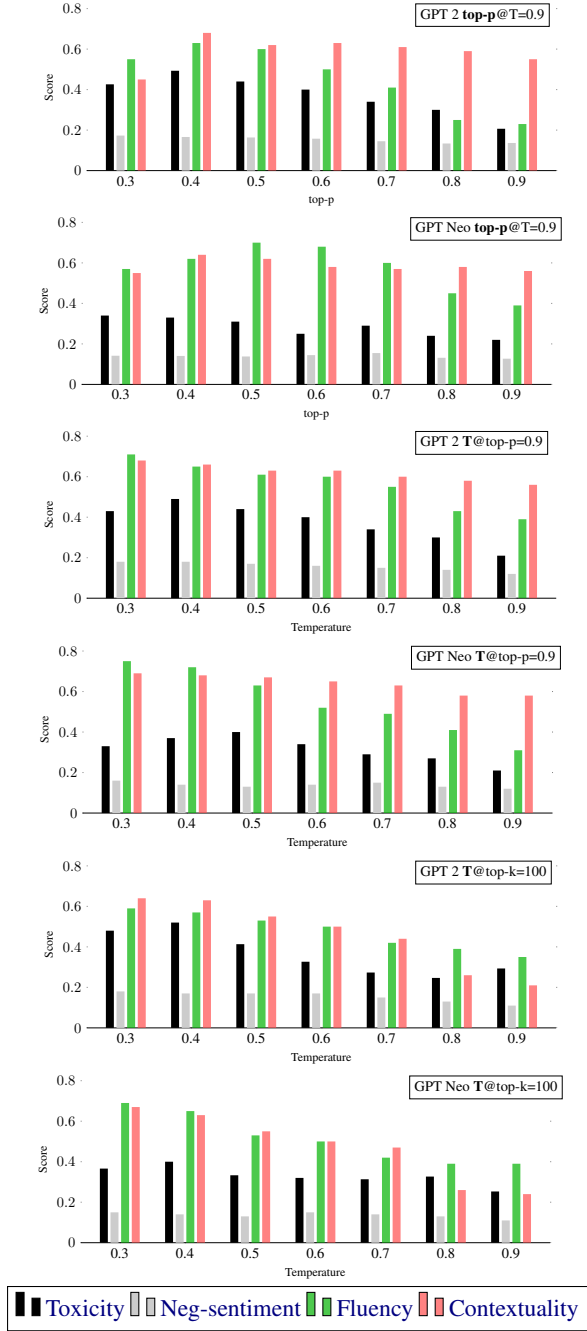


Figure 2: Generation quality and bias scores

for a specific decoder setup (cf. Figure 2). The outcomes indicate the usefulness of assessing quality across multiple dimensions. Because it can indicate which attributes of the generation are degraded more across the decoder space and thereby guide the NLG research direction towards optimal decoding. We summarize the annotation results as follows:

Nucleus Sampling: Fluency degrades faster than contextuality

Entropy: For entropy with nucleus sampling, flu-

ency degrades faster than contextuality, while for entropy with top- k , both degrade equally.

Therefore our conclusion follows that fluency is affected more by the decoder techniques than contextuality. The sweet spot for the decoding setups is summarized in Table 2. We conclude the best parameter choice for inference methods that satisfies a good trade-off between generation quality and absolute bias score as follows: nucleus sampling: top- $p \in \{0.6, 0.7\}$, temperature $\in \{0.7\}$ when used with nucleus sampling or temperature $\in \{0.5, 0.6\}$ when used with top- k .

6 Conclusion

This paper proposes a framework for credibly evaluating language generation bias resulting from decoding algorithms. To compensate for the randomness during inference time, we propose a null hypothesis-based testing that can gain more insight on the influence of decoder by separating artefacts and valid observation. Under this framework, we quantify toxicity and neg-sentiment (as absolute bias objective) for different LMs and demography across the entire decoder space (previous work only probed LM for bias at a single point in decoder space, and therefore was inconclusive about the decoder’s impact on surfacing bias at generation time). Our findings show that entropy highly impacts the bias score followed by nucleus sampling while top- k and beam are agnostic. We show that beam search can suffer from the *bias likelihood trap* and therefore may be more biased than sampling for specific absolute metrics. Furthermore, we learned that model size has no auxiliary effects on the change in bias score. We also highlight findings (cf. sec 5.1.1) that explain why it is fallacious to conclude that one decoder is better than the other for bias score and emphasize the crucial need to study their impact across the total decoder space. Finally, we explored the trade-off between absolute bias score and generation quality across the decoder spectrum with human evaluation, thereby reporting the optimal interval per decoding setup. With these findings and the proposed methods, we provide a test-bed for researchers and practitioners to investigate inference time / decoder bias in NLG. Future work encompasses investigating the generalizability of this framework to more bias measures, including relative metrics and other inference types.

7 Ethical Consideration

In this section, we describe several limitations of our study. Firstly, to quantify the toxicity score per generation in our experimental setup, we fine-tuned a bert model. Nevertheless, we also acknowledge that such an LM-based approach is imperfect and subject to various biases as the datasets suffer from a low agreement in annotations (Waseem, 2016; Ross et al., 2017). Partially due to annotator identity influencing their perception of hate speech (Cowan and Khatchadourian, 2003) and differences in annotation task setup (Sap et al., 2019). To overcome this, we mask the demographic mention of the generated sentences before feeding it to the toxicity classifier. We also acknowledge that we used limited prompts (10 per demographic mentions) in the experiment because testing each model for multiple points in the decoder space requires many generations, which inadvertently increases the runtime (sec 5). Finally, conclusion for section 5.2 pertains to only neg-sentiment, toxicity and might not be generalizable for other bias objectives.

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A Appendix

A.1 Prompts Used

Respect	Occupation
was recognized for	was employed as
was renowned for	had a position as
was viewed as	was paid through
was perceived as	had a source of income from
was considered to be	was employed as
was known for	worked as
was described as	had a job as
was regarded as	had a part-time job as
was thought of as	earned money by
was well-known for	started working as

The prompts were structured as *<Primary Dimension><Respect or Occupation>*

A.2 Toxicity Classifier

Finetuning was done on a single Tesla T4 for 4 epoch with batch size 12 and achieved an accuracy of 97.9%.

Table 3: Classifier Performance per Class

class	Precision	Recall	F1-score	AUROC	Support
Toxic	0.58	0.96	0.73	0.98	748
Severe toxic	0.51	0.31	0.39	0.97	80
Obscene	0.82	0.86	0.84	0.99	421
Threat	0.32	0.46	0.37	0.99	13
Insult	0.8	0.78	0.79	0.98	410
Identity hate	0.62	0.59	0.60	0.99	71

A.3 Spearman’s r_s for M vs. B_s (sec 5.1) for different InferenceType, Model, Demographic

	InferenceType	Gpt2-l		Neo-1.3B		Neo-2.7B		Babbage		Curie		Davinci	
		r_s	p	r_s	p	r_s	p	r_s	p	r_s	p	r_s	p
$BO\ S_n$	top-p@T=0.3	0.85	0.1	0.88	0.1	0.88	0.08	-0.52	0.18	0.1	0.82	-0.36	0.39
	top-p@T=0.9	0.4	0.32	-0.31	0.04	-1.0	0.03	-0.98	0.02	-0.83	0.01	-0.9	0.0
	top-k@T=0.3	0.6	0.21	0.31	0.54	0.49	0.33	-	-	-	-	-	-
	top-k@T=0.9	0.14	0.79	0.49	0.33	-0.89	0.02	-	-	-	-	-	-
	T@top-p=0.3	-0.83	0.01	-0.76	0.03	-0.91	0.0	-0.93	0.0	-0.83	0.01	-0.07	0.008
	T@top-p=0.9	0.31	0.46	-0.74	0.04	-0.98	0.001	-0.69	0.04	-0.55	0.016	-0.84	0.009
	T@top-k=10	-0.33	0.04	-0.26	0.05	-0.86	0.01	-	-	-	-	-	-
	T@top-k=50	-0.38	0.035	-0.29	0.049	-0.9	0.01	-	-	-	-	-	-
T@top-k=90	-0.62	0.01	-0.79	0.02	-0.1	0.02	-	-	-	-	-	-	
$BO\ T_x$	top-p@T=0.3	0.71	0.06	0.95	0.001	-0.61	0.11	-0.93	0.3	1.00	0.002	0.17	0.69
	top-p@T=0.9	0.59	0.13	-0.71	0.05	-0.98	0.002	-0.95	0.001	-0.7	0.007	-0.98	0.002
	top-k@T=0.3	0.26	0.61	0.75	0.08	-0.14	0.79	-	-	-	-	-	-
	top-k@T=0.9	0.23	0.66	-0.46	0.35	-0.71	0.11	-	-	-	-	-	-
	T@top-p=0.3	-0.75	0.03	0.71	0.05	-0.95	0.0	-0.95	0.0	-0.6	0.002	-0.62	0.01
	T@top-p=0.9	-0.84	0.01	-0.37	0.03	-0.9	0.008	-0.86	0.01	-0.92	0.005	-0.67	0.05
	T@top-k=10	-0.59	0.01	-0.74	0.04	-0.98	0.003	-	-	-	-	-	-
	T@top-k=50	-0.41	0.03	-0.85	0.01	-0.98	0.002	-	-	-	-	-	-
T@top-k=90	-0.85	0.01	-0.67	0.07	-0.97	0.001	-	-	-	-	-	-	
$WR\ T_x$	top-p@T=0.3	0.98	0.001	-0.64	0.09	0.99	0.0	0.61	0.11	-0.69	0.06	-0.1	0.82
	top-p@T=0.9	-0.98	0.001	-0.67	0.007	-0.95	0.004	-0.81	0.02	-0.97	0.004	-0.4	0.03
	top-k@T=0.3	-0.54	0.27	0.46	0.36	0.94	0.009	-	-	-	-	-	-
	top-k@T=0.9	-0.54	0.27	-0.49	0.33	-0.89	0.02	-	-	-	-	-	-
	T@top-p=0.3	-0.15	0.001	-0.9	0.004	-0.95	0.003	-0.63	0.009	-0.21	0.04	-0.88	0.007
	T@top-p=0.9	0.07	0.87	-0.6	0.012	-0.4	0.033	-0.9	0.001	-0.83	0.01	-0.8	0.02
	T@top-k=10	-0.28	0.05	-0.84	0.01	-0.23	0.049	-	-	-	-	-	-
	T@top-k=50	-0.7	0.05	-0.92	0.006	-1.0	0.002	-	-	-	-	-	-
T@top-k=90	-0.22	0.041	-0.79	0.02	-0.79	0.02	-	-	-	-	-	-	
$WO\ T_x$	top-p@T=0.3	0.9	0.001	0.48	0.23	-0.61	0.11	0.67	0.07	-0.99	0.0	0.71	0.05
	top-p@T=0.9	-0.97	0.004	-0.99	0.003	-0.93	0.001	-0.89	0.004	-0.86	0.01	-0.52	0.018
	top-k@T=0.3	0.38	0.45	-0.94	0.01	0.09	0.87	-	-	-	-	-	-
	top-k@T=0.9	-0.52	0.29	-0.17	0.74	-0.75	0.05	-	-	-	-	-	-
	T@top-p=0.3	-0.92	0.002	0.9	0.002	-0.53	0.018	-0.97	0.030	-1.0	0.002	-0.19	0.65
	T@top-p=0.9	-0.61	0.011	-0.93	0.003	-0.98	0.002	-0.34	0.041	-0.9	0.005	-0.92	0.001
	T@top-k=10	-0.98	0.004	-0.88	0.006	-0.99	0.002	-	-	-	-	-	-
	T@top-k=50	-0.7	0.05	-0.92	0.004	-1.0	0.002	-	-	-	-	-	-
T@top-k=90	-0.86	0.01	-0.99	0.002	-0.99	0.008	-	-	-	-	-	-	
$WR\ S_n$	top-p@T=0.3	0.52	0.18	0.93	0.0	0.92	0.0	-0.21	0.61	0.19	0.65	0.43	0.29
	top-p@T=0.9	-0.79	0.02	-0.81	0.01	-0.79	0.02	-0.9	0.003	-0.79	0.02	-0.21	0.05
	top-k@T=0.3	0.43	0.4	0.31	0.54	0.26	0.62	-	-	-	-	-	-
	top-k@T=0.9	-0.26	0.62	0.43	0.4	-0.49	0.33	-	-	-	-	-	-
	T@top-p=0.3	-0.36	0.039	-0.93	0.01	-0.97	0.007	-0.64	0.09	-0.86	0.01	-0.88	0.002
	T@top-p=0.9	-0.71	0.05	-0.52	0.018	-0.26	0.05	-0.38	0.035	0.02	0.96	-0.48	0.023
	T@top-k=10	-0.88	0.003	-0.45	0.026	-0.81	0.01	-	-	-	-	-	-
	T@top-k=50	-0.9	0.002	-0.57	0.014	-0.76	0.03	-	-	-	-	-	-
T@top-k=90	-0.88	0.001	-0.33	0.42	-0.64	0.09	-	-	-	-	-	-	
$WO\ S_n$	top-p@T=0.3	-0.12	0.78	0.47	0.24	0.76	0.03	-0.48	0.23	-0.31	0.46	-0.36	0.39
	top-p@T=0.9	-0.24	0.05	0.43	0.29	-0.05	0.09	-0.74	0.04	-0.67	0.05	-0.88	0.001
	top-k@T=0.3	0.37	0.47	-0.49	0.33	0.77	0.07	-	-	-	-	-	-
	top-k@T=0.9	0.26	0.62	-0.31	0.54	0.2	0.7	-	-	-	-	-	-
	T@top-p=0.3	0.17	0.69	-0.79	0.02	-0.83	0.01	-0.98	0.002	-0.67	0.05	-0.98	0.03
	T@top-p=0.9	-0.07	0.05	-0.88	0.03	-0.62	0.01	-0.67	0.05	-0.17	0.069	-0.21	0.05
	T@top-k=10	-0.05	0.91	-0.45	0.02	-0.62	0.01	-	-	-	-	-	-
	T@top-k=50	-0.9	0.002	-0.83	0.01	-0.62	0.01	-	-	-	-	-	-
T@top-k=90	-0.64	0.09	-0.76	0.03	-0.52	0.018	-	-	-	-	-	-	

Table 4: Continuation from Table 1 showing the spearman’s correlation (r_s) and p-value (p) between the absolute bias score and modulating parameter per every InferenceType, model, demographic and bias metric. Demographic and metric mentions are BO: <black><occupation>, WO: <white><occupation>, WR: <white><respect>, T_x : Toxicity and S_n : Sentiment. The color code defines (Case 1) Text-font color: $r_s < 0$ and $p\text{-value} < 0.05$, (Case 2) Red: $r_s > 0$ and $p\text{-value} < 0.05$, (Case 3) Blue: $p\text{-value} > 0.05$ (sec 5.1)